

**Mid Term Review****Completely Factor and Graph #4**

1. A) Completely Factor  $x^4 - 18x^2 + 81$  \_\_\_\_\_

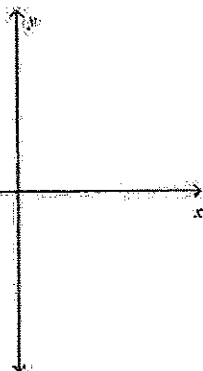
B) What are the zeros \_\_\_\_\_

C) What is the Y intercept? \_\_\_\_\_

D) Degree = \_\_\_\_\_

E) What is the end behavior  $x \rightarrow -\infty$   $f(x) \rightarrow$  \_\_\_\_\_  
 $x \rightarrow +\infty$   $f(x) \rightarrow$  \_\_\_\_\_

Sketch the Graph



2. Factor  $x^3 - 64$

Answer \_\_\_\_\_

• What values of  $x$  make the equation true?

$$\frac{5}{x+5} = \frac{10}{x^2-25}$$

3. A rock is dropped from a bridge from a height of 576 feet. The height of the bridge is modeled by the equation  $h(t) = -16t^2 + 784$ , where  $h(t)$  is the height of the bridge in feet and  $t$  is the time in seconds. When will the rock hit the water. (Show your work by factoring and include proper units.

A) Factored Form \_\_\_\_\_

B) Answer  $t =$  \_\_\_\_\_

(4) Find the Quotient.

$$(x^3 + 2x^2 - 22x - 45) \div (x + 5)$$

show work.

(6)

$$(x^3 - x^2 - x - 2) \div (x - 2)$$

Answer \_\_\_\_\_

(5) Divide.

$$(2x^3 - 14x + 10) \div (x + 3)$$

Answer \_\_\_\_\_

Quotient \_\_\_\_\_ B) Is  
the divisor a factor? \_\_\_\_\_ List the  
Divisor

C) Why or Why  
Not? \_\_\_\_\_

7. Use synthetic division to divide.

$$(3x^3 + 19x^2 + 30x + 8) \div (x + 4)$$

Answer \_\_\_\_\_

Name: \_\_\_\_\_

ID: A

Factor the polynomial completely. You Must Show Work on 9-11

8.  $49y^2 - 36$

Answer: \_\_\_\_\_

9.  $x^3 - 5x^2 + 4x$

Answer: \_\_\_\_\_

10.  $8x^2 - 6x - 27$

Answer: \_\_\_\_\_

11.  $15x^3 + 5x^2 + 15x + 5$

Answer: \_\_\_\_\_

12. A) Completely write in  $5x^3 + 5x^2 - 30x$  in factored form.

A) \_\_\_\_\_

B) What are the zeros \_\_\_\_\_

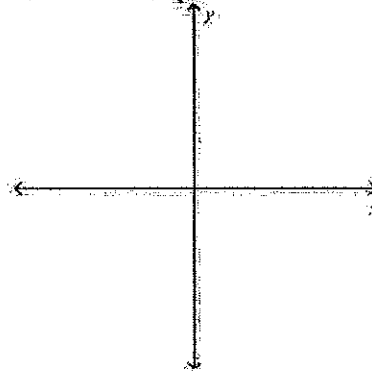
C) What is the Y intercept? \_\_\_\_\_

D) Degree = \_\_\_\_\_

E) What is the end behavior

 $x \rightarrow -\infty f(x) \rightarrow \underline{\hspace{1cm}}$   $x \rightarrow +\infty f(x) \rightarrow \underline{\hspace{1cm}}$ 

Sketch the Graph



Name: \_\_\_\_\_

ID: A

 $f(x) = (x-2)(x+3)(x+1)?$ 

13. The table shows the growth of a dandelion plant over the course of 5 days. What is the average rate of change in the growth of the Dandelion from Day 1 to Day 4? Round your answer to the nearest hundredth.

Day	1	2	3	4	5
Height of Plant (In Inches)	.20	.25	.35	.50	.70

14. What is the remainder when  $f(x) = x^3 + 5x^2 - 2x - 6$  is divided by  $(x-2)$

15. What is the x-intercept of  $x^4 + 10x^3 + 21x^2 + 10x - 8$
16. Is  $(x+2)$  a factor of your reasoning.

17. The table shows the daily account balance of a checking account.

Day	1	2	3	4	5
Account Balance (in dollars)	355.75	325.16	317.22	280.68	154.37

What is the average rate of change in the account balance from Day 1 to Day 4.

18.

19. A function  $h(x)$  is used to represent the number of items sold at a store during business hours  $x$ . The table shows some values for the function.

$x$	0	1	2	3	4
$h(x)$	0	15	23	37	?

The average rate of change of  $h(x)$  over the interval  $1 \leq x \leq 4$  is 21.

What is the missing value in the table?

20. A polynomial,  $f(x)$ , is divided by four different linear expressions, as listed in the table. The resulting remainders after the division by each linear expression are as shown in the table.

Linear Expression	Remainder
$x-1$	2
$x+1$	0
$x-3$	4
$x+3$	0

What are possible roots?

21. Select the factors of
- $x^3 + 5x^2 - 5x - 25$

Mark the box of each factor

	$x - 5$	$x + 5$	$x - 10$	$x + 10$	$x^2 + 5$
$x^3 + 5x^2 - 5x - 25$					

22. The difference of cubes identity will be used to determine the difference between 216 and 64.

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

$$216 - 64 = (2)(36 + 24 + 16)$$

What values of a and b should be used? Select the two that apply.

M.  $a = 6$ P.  $a = 10$ R.  $a = 18$ S.  $b = 4$ T.  $b = 8$ V.  $b = 16$ 

23. Given the polynomial
- $2x^2 + 11x - 15$
- , determine the values of x where the graph of the polynomial crosses the x axis.

Select one value from each box to correctly complete the following statements.

One Solution to x is

- A) -2.5  
B) 2.5  
C) 5  
D) -5

The Other Solution to x is

- E) -1.5  
F) 3  
G) 1.5  
H) -3

27. Consider the expression
- $(x^2 - 9)(x - 2)$
- 
- Select all the values of x for which
- $(x^2 - 9)(x - 2) = 0$

A) -2	B) 3	C) 1	D) -2
E) 0	F) 2	G) -3	H) 9

24. Select all expressions that are equivalent to

$$3x^5 - 6x^4y + 3x^3y^2$$

A)  $3x^3(x - y)$

B)  $3x^3(x^2 - 2xy - y^2)$

C)  $3x^3(x + y)^2$

D)  $3x^3(x - y)(x + y)$

E)  $3x^3(x - y)(x^2 - y)$

25. Select all the solutions to the equation

$$x^2 + 2x + 10 = 0$$

A) 2

B) 5

C)  $-1 + 3i$

D)  $-1 - 3i$

E)  $-1 - i\sqrt{11}$

F)  $-1 + i\sqrt{11}$

26. Which is the correct factorization of the expression
- $x^4 - 256$

Factor.